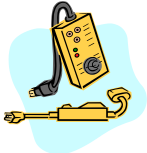


# VOLTAGE DOUBLER AND RECTIFIERS WITH CAPACITIVE FILTER



## I. OBJECTIVES

- To understand how voltage multipliers (doubler) can be built using simple DC circuits.
- To determine how the frequency of the input voltage influences the rectified output voltage.



## II. COMPONENTS AND INSTRUMENTATION

You will use a breadboard, semiconductor diodes of 1N4184 type (the stripe indicates the cathode), 330 nF capacitors and a 10 k $\Omega$  resistor. Because you will apply and measure ac voltages, you will need a signal generator and a dual channel oscilloscope.



## III. THEORETICAL ASPECTS

### 1. Voltage doubler

Think of it as a cascading connection between an upward translation two-port network (from  $v_I$  to  $v_{O1}$ ) and a positive peak detector (from  $v_{O1}$  to  $v_O$ ).

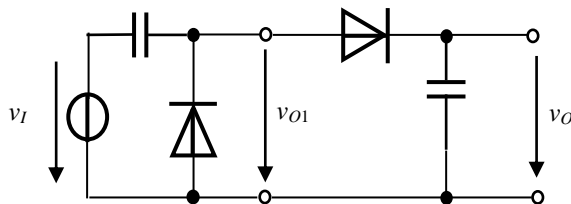


Fig. 1. Voltage doubler using a translation circuit and a peak detector.

The waveforms in steady-state regime, in the case of a sinusoidal input signal with  $\hat{V}_I$  amplitude are plotted in Fig. 2.

### 2. Half-wave rectifiers with capacitive filter

Rectifiers with D and R generate an output voltage of a single sign, but it has a considerable variation, equal to the amplitude of the input signal. To obtain a continuous voltage, we must smoothen these variations by adding a filtering capacitor (see Fig. 3).

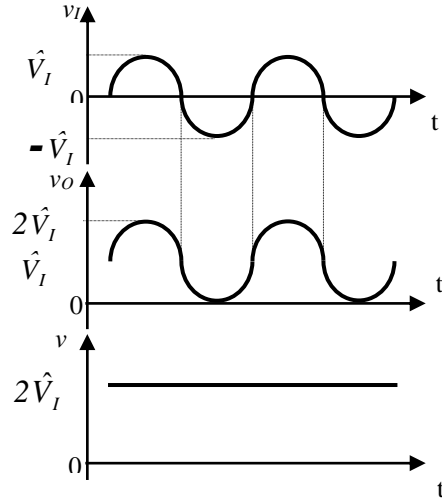


Fig. 2. Waveforms in steady-state for the doubler in Fig. 1

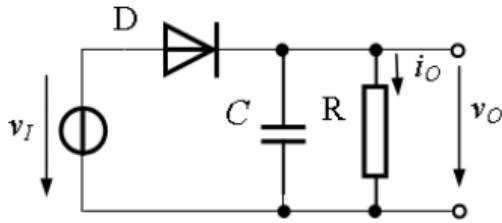


Fig. 3. Half-wave rectifier with capacitive filter

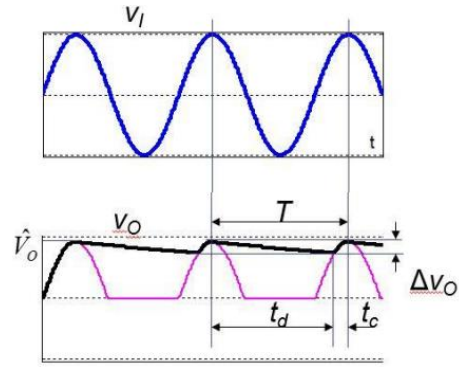


Fig. 4. Waveforms for half-wave rectifier with capacitive filter

The circuit can be seen also as a positive peak detector loaded with  $R$ . In actual practical situations, such as the design of power supplies a load resistance will be inherently present. If the input voltage is an alternative sinusoidal one, between two consecutive peaks of  $v_I$ , the capacitor will discharge through  $R$  and  $v_O$  will go down, unlike the situation without  $R$  when  $v_O$  was constant. The waveforms in steady-state for the circuit in Fig. 3 are plotted in Fig. 4. The time constant of the circuit,  $RC$ , should be much greater than the period  $T$  of the signal,  $RC \gg T$ . Note that the output is no longer a constant dc voltage but it may be considered as being composed on a dc voltage on which an ac component, called *ripple*, is superimposed.

We specify the following:

- The diode  $D$  conducts for short time intervals  $\Delta t_c$ , close to the positive peaks of  $v_I$ . We neglect the voltage drop across the conducting diode. The capacitor charges with an electric charge equal to the one lost on the longest duration of the discharge,  $\Delta t_d$ .

$$v_c(t) = (1 - e^{-\frac{t}{RC}})V_\infty + V(0) \cdot e^{-\frac{t}{RC}}$$

- When  $D$  (off),  $C$  discharges through  $R$  and in this way  $v_O$  drops exponentially with the time constant  $RC$ . At the end of the discharge interval  $\Delta t_d$ , which is almost equal with  $T$ ,  $v_O = \hat{V}_I - \Delta v$ , where  $\Delta v$  is the peak to peak value of the ripple of the output voltage. If  $RC \gg T$ ,  $\Delta v$  is small. A special attention will be paid to this ripple  $\Delta v$ .

We remind the expression of the voltage across the capacitor.

$$v_c(t) = (1 - e^{-\frac{t}{RC}})V_\infty + V(0)e^{-\frac{t}{RC}}$$

Let us assume the initial time moment,  $t=0$  as being the moment when the discharge of the capacitor begins ( $v_I$  at the maximum value), therefore  $V(0) = \hat{V}_I$ .  $V_\infty$  is the value at which the voltage on the capacitor could finally reach, if the input signal will disappear,  $V_\infty = 0V$ . The time interval in which we are interested is the one of the capacitor's discharge  $t = \Delta t_d$ , when the value of the voltage is:

$$v(\Delta t_d) = \hat{V}_I - \Delta v$$

We obtain:

$$\hat{V}_I - \Delta v = \hat{V}_I e^{-\frac{\Delta t_d}{RC}} \approx \hat{V}_I e^{-\frac{T}{RC}}$$

Because  $RC \gg T$  we can use the approximation:

$$e^{-\frac{T}{RC}} \approx 1 - \frac{T}{RC}$$

$$\hat{V}_I - \Delta v = \hat{V}_I - \frac{T}{RC} \hat{V}_I$$

$$\Delta v = \frac{T}{RC} \hat{V}_I$$

The higher the time constant  $RC$  (usually by choosing a large value for  $C$ ), the smaller is the ripple, so  $v_O$  is closer to a smooth continuous voltage.

*Remark:* An alternative interpretation of the previous approximation is that, on the intervals  $\Delta t_d$  we consider that the discharge of the capacitor happens at a constant current  $I_O = \frac{\hat{V}_I}{R}$ . This interpretation holds as long as  $\Delta v \ll \hat{V}_I$

$$\Delta v = \frac{T}{C} I_O = \frac{T}{RC} \hat{V}_I$$

If we want to use the frequency  $f$  of the voltage:

$$\Delta v = \frac{1}{fC} I_O = \frac{1}{fRC} \hat{V}_I$$



## IV. PREPARATION

### 1.P. Voltage doubler

The questions address the circuit in Fig. 5.

- What is the function of the circuit consisting of  $D_1$  and  $C_1$ , with the output  $v_{O1}(t)$ ?
- Plot  $v_I(t)$ ,  $v_{O1}(t)$  and  $v_{C1}(t)$  in steady state, if  $v_I(t)$  is a sinusoidal voltage with 10 V amplitude.
- What is the function of the circuit consisting of  $D_2$  and  $C_2$ , with the output  $v_O(t)$ ?
- Plot  $v_I(t)$ ,  $v_O(t)$  and  $v_{D2}(t)$  in steady state, if  $v_I(t)$  is a sinusoidal voltage with 10 V amplitude.

## 2.P. Half-wave rectifier with capacitive filter

The questions address the circuit in Fig. 6.

- Plot  $v_I(t)$  and  $v_O(t)$ , if  $v_I(t)$  is a sinusoidal voltage with 10 V amplitude.
- Compute the output voltage ripple  $\Delta v_O$  for  $f = 100$  Hz and  $f = 1$  kHz.
- What is the effect of the frequency on  $v_O(t)$  and  $\Delta v_O$ ?

## 3.P. Spatial maximum circuit with capacitive filter

The questions address the circuit in Fig. 7.

- Plot  $v_A(t)$ ,  $v_B(t)$  and  $v_O(t)$ , if  $v_A(t)$  is a sinusoidal voltage with 10 V amplitude, and  $v_B(t)$  is a dc voltage, 5 V amplitude.
- Can the output voltage ripple  $\Delta v_O$  be computed using the same equation as for the previous circuit? Justify your answer.

# V. EXPLORATIONS AND RESULTS



## 1. Voltage doubler Exploration

Build the circuit shown in Fig. 5.

- At the input of the circuit apply a sinusoidal voltage with 500 Hz frequency and 10 V amplitude obtained from the signal generator.
- $v_I(t)$ ,  $v_{O1}(t)$  and  $v_O(t)$  are visualized on the oscilloscope. Because you can visualize only two signals simultaneously you will visualize first  $v_I(t)$  and  $v_{O1}(t)$  and then  $v_I(t)$  and  $v_O(t)$ , using the DC setting for both channels.

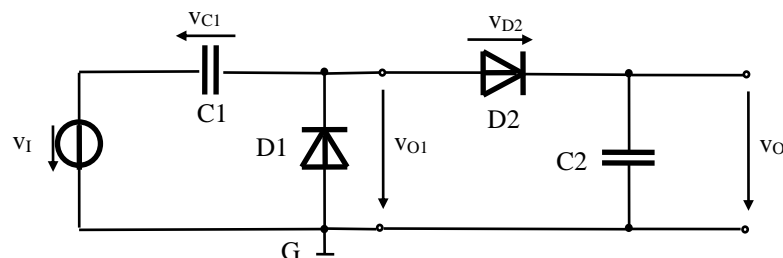


Fig. 5. Voltage doubler



## Results

- Draw the waveforms for  $v_I(t)$ ,  $v_{O1}(t)$ ,  $v_O(t)$ ,  $v_{C1}(t)$  and  $v_{D2}(t)$  for 10 V amplitude of the input voltage.

## 2. Half-wave rectifier with capacitive filter

### Exploration

Build the circuit shown in Fig. 6.

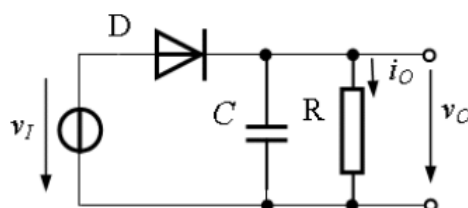


Fig. 6. Half-wave rectifier with capacitive filter

- At the input of the circuit apply a sinusoidal voltage with 100 Hz frequency and 10 V amplitude obtained from the signal generator.
- Visualize  $v_I$  and  $v_O$  on the oscilloscope, using the DC setting for both channels.
- Compute the output voltage ripple, by reading the values from the oscilloscope.
- Change the frequency of the input voltage to  $f = 1$  kHz. Recompute the output voltage ripple, by reading the values from the oscilloscope.



### Results

- Plot of  $v_I(t)$ ,  $v_O(t)$ .
- Computed output voltage ripple for  $f = 100$  Hz and  $f = 1$  kHz.
- How does the frequency influence  $v_O(t)$  and  $\Delta v_O$ ?

## 3. Spatial maximum circuit with capacitive filter



### Exploration

Build the circuit shown in Fig. 7

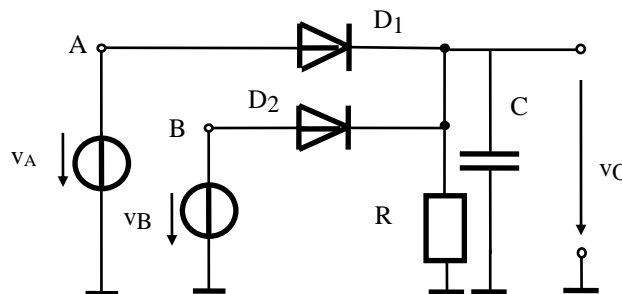


Fig. 7. Spatial maximum circuit with capacitive filter

- At the input of the circuit apply  $v_A$  - sinusoidal voltage with 100 Hz frequency and 10 V amplitude obtained from the signal generator, and  $v_B = 5$  V from the power supply.
- Visualize  $v_A$  and  $v_O$  on the oscilloscope, using the DC setting for both channels.
- Compute the output voltage ripple, by reading the values from the oscilloscope.
- Change the frequency of the input voltage to  $f = 1$  kHz. Recompute the output voltage ripple, by reading the values from the oscilloscope.



### Results

- Plot of  $v_A(t)$ ,  $v_O(t)$ .
- Computed output voltage ripple for  $f = 100$  Hz and  $f = 1$  kHz.
- How does the frequency influence  $v_O(t)$  and  $\Delta v_O$ ?
- How does  $\Delta v_O$  change, compared to the previous circuit?

### REFERENCES

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